

# DARK MATTER VERSUS COSMOLOGICAL CONSTANT

## DARK MATTER IN ASTROPHYSICS

- Source of gravitational field, but
- nor source nor transmitter of electromagnetic radiation

## DARK PARTICLES

- Energy-momentum conservation
- Conservation of charges
- Symmetry partners
- Topological peculiarities
- Virtual particles: Vacuum

## COSMOLOGICAL CONSTANT

- Curvature-matter balance
- Zero-point curvature: No phase transitions
- Vacuum: Phase transitions

# THE FRIEDMANN EQUATION

## SPACE-TIME CURVATURE = MASS DENSITY

---

EXPANSION RATE	+	SPACE CURVATURE	=	VIRTUAL MASS DENSITY	+	REAL MASS DENSITY
-------------------	---	--------------------	---	----------------------------	---	-------------------------

---

$$\left(\frac{1}{R} \frac{dR}{dt}\right)^2 + \frac{kc^2}{R^2} = \frac{\Lambda c^2}{3} + \frac{8\pi G}{3} \varrho$$


---

$$h^2[z] + \kappa_0(1+z)^2 = \lambda_0 + \sum_n \Omega_{n0}(1+z)^n$$


---

$$1 + \kappa_0 = \lambda_0 + \sum_n \Omega_{n0}$$


---

Balancing the expansion rate by

- **radiation** :  $n = 4$
- **dust (free streaming dark matter or interacting dust with negligible pressure)**:  $n = 3$
- **gas of strings**:  $n = 2$  (like curvature)
- **gas of domain walls**:  $n = 1$
- **vacuum**:  $n = 0$  (like cosmological constant)

Kardashov,N.S. 1990

# LACK OF GRAVITATING MASS

- **General reviews**

Peebles,P.J.E., Schramm,D.N., Turner,E.L., Kron,R.G. 1991  
Schramm,D.N. 1992

- **Rotation curves of Galaxies**

Ashman,Keith M. 1992  
Brainerd,T.G., Villumsen,J.V. 1992  
Brainerd,T.G., Villumsen,J.V. 1992

- **Galaxy formation**

Dekel,A., Silk,J. 1986

- **Velocity dispersion in groups of galaxies**

Ninkovich,S., Chernin,A., Shakenov,M. 1990

- **Polar rings in hypergalaxies**

Einasto,Jaan, Haud,Urmas, Joeveer,Mihkel, Kaasik,Ants 1976  
Sackett,P.D., Sparke,L.S. 1990

- **Velocity dispersion of clusters of galaxies**

Kauffmann,G., White,S.D.M. 1992

- **Growth of primordial post-recombination perturbations (Time problem of primeval structure formation)**

Davis,M., Summers,F.J., Schlegel,D. 1992

- **Extra power on large scales**

Davis,M., Efstathiou,G., Frenk,C.S., White,S.D.M. 1992

- **Friedmann balance of cosmic expansion**

Guth,Alan H. 1981

## MASS DENSITIES

---

<b>Reduced masses</b>	$\frac{M}{L}$	$\left[ \frac{M_\odot}{L_\odot} \right]$	$\varrho$	$\left[ \frac{M_\odot}{\text{Mpc}^3} \right]$	$\Omega = \frac{\varrho}{\varrho_{\text{crit}}}$
-----------------------	---------------	--	-----------	---	--

---

Microwave background		<b>7</b>	<b>10<sup>-3</sup></b>	<b>2.5</b>	<b>10<sup>-5</sup>h<sup>-2</sup></b>	
Luminous matter	<b>5</b>	<b>h</b>	<b>0.65</b>	<b>h<sup>2</sup></b>	<b>2.4</b>	<b>10<sup>-3</sup></b>
Galaxy halos	<b>10</b>	<b>h</b>	<b>1.11</b>	<b>h<sup>2</sup></b>	<b>4.7</b>	<b>10<sup>-3</sup></b>
Hypergalaxy halo	<b>25</b>	<b>h</b>	<b>2.77</b>	<b>h<sup>2</sup></b>		<b>0.01</b>
Baryonic matter			<b>2.95</b>		<b>0.011</b>	<b>h<sup>-2</sup></b>
Cluster halo	<b>325</b>	<b>h</b>	<b>36</b>	<b>h<sup>2</sup></b>		<b>0.13</b>
Critical density			<b>273</b>	<b>h<sup>2</sup></b>		<b>1</b>

---

# DARK MATTER TYPES

- **Review**

Gelmini,G.B. 1992

- **Ordinary particles  $SU(3) \times SU(2) \times U(1)$**

Persic,Massimo, Salucci,Paolo 1992

- Dark baryons (brown dwarfs, gas, stillborn galaxies)
- Massive Neutrinos
- WIMPs (100 GeV)

- **Particles beyond  $SU(3) \times SU(2) \times U(1)$**

- **Supersymmetric partners**

Domenech,G., Levinas,M., Umerez,N. 1991

Berezinsky,V.S., Gurevich,A.V., Zybin,K.P. 1992 :

- \* **Gravitinos**

Frieman,J.A., Giudice,G.F. 1989

- \* **Neutralinos**

Gelmini,G.B. 1992

- **Shadow matter**

Kolb,E.W., Seckel,D., Turner,M.S. 1985

Sciama,D.W. 1990

- **Cryptons**

Ellis,J., Lopez,J.L., Nanopoulos,D.V. 1990

- **Mirror baryons**

Hodges,H.M. 1993

- **Massive BH**

Hut,P., Rees,M.J. 1992

- **Maximons**

Markov,M.A. 1993

- **Topological particles:**

- **Strings**

Arnowitt,R., et al. (eds.) 1990

- **Axions ( $10^{-5}$  eV)**

Turner,M.S. 1990

- **Textures**

Silk,J., Juszkiewicz,R. 1991

## DIRECT AND INDIRECT OBSERVATIONS

- Particle detection (underground physics)  
Caldwell,D.O. 1992
- Limits on particles by observation of the galactic halo  
Berezinsky,V.S., Gurevich,A.V., Zybin,K.P. 1992
- Long-range interaction  
Stubbs,C.W. 1993
- Influence on big bang nucleosynthesis  
Hagelin,J.S., Parker,R.J.D. 1990
- Influence on chemical evolution  
Matteucci,F. 1992
- Influence on density fluctuations  
Taylor,A.N., Rowan-Robinson,M. 1992
- Influence on structure formation  
Vandalen,A., Schaefer,R.K. 1992  
Davis,M., Summers,F.J., Schlegel,D. 1992

## ALTERNATIVES

- Magnetic fields instead of dark matter  
Binney,James 1992  
Fahr,H.J. 1990
- Cosmological constant  
Gessner,E. 1992
- Non-Newtonian forces  
Dar,A. 1992  
Gerhard,O.E., Spergel,D.N. 1992  
Gradwohl,B.A., Frieman,J.A. 1992
- low density  
Bahcall,Neta A., Cen,Renyue 1992  
Davis,M., Efstathiou,G., Frenk,C.S., White,S.D.M. 1992  
Liebscher,D.-E., Priester,W., Hoell,J. 1992  
Liebscher,D.-E., Priester,W., Hoell,J. 1992

# COSMOLOGICAL CONSTANT AND VACUUM ENERGY

- Constant: Geometrical quantity, measurement only by geometry  
To first order in redshift: deceleration parameter

$$q = \frac{1}{2} \frac{dh[z]}{dz} - 1 \quad (1)$$

- Vacuum: subject to phase transitions

## VACUUM PHASE TRANSITIONS

- Inflation

Guth, Alan H. 1981

- Late-type cosmological phase transitions, no more exotic than GUT

Schramm, D. 1991

- Effective (classical) vacua (for instance S. Antoci)

- Kaluza-Klein phase transitions

Bengtson, Ingemar, Boström, Olaf 1992

## COSMOLOGICAL CONSTANT

- Review

Carroll, S.M., Press, W.H., Turner, E.L. 1992

Peebles, P.J.E., Schramm, D.N., Turner, E.L., Kron, R.G. 1991

- Zero cosmological constant

Carlberg, R.G. 1991 Merging of galaxies  $\propto (1+z)^5$

Kochanek, C.S. 1992 Gravitational lensing

Kellermann, K.I. 1993 Size of ejecta of radio galaxies

- Nonzero cosmological constant

Fukugita, M., Lahav, O. 1991 Lyman-alpha at low redshift

Fukugita, M., Takahara, F., Yamashita, K., Yoshii, Y. 1990  $m[z]$  in the blue band

Turner, Edwin L., Ikeuchi, Satoru 1992 Evolution of forest density

- General discussion of observational points

Kauffmann, G., White, S.D.M. 1992

Fukugita, M., Futamase, T., Kasai, M. 1990

Lahav, O., Lilje, P.B., Primack, J.R., Rees, M.J. 1991

Efstathiou, G., Sutherland, W.J., Maddox, S.J. 1990

# QUASAR ABSORPTION FOREST: STRUCTURE

**Density of absorbers along the line of sight:**

$$dN \propto \sigma d\chi. \quad (2)$$

**Evolution in number density**

$$n[z] dz = \sigma[z] \frac{dz}{h[z]}. \quad (3)$$

**Evolution in comoving size and cross-section**

$$L_{\text{comoving}} = L_{\text{physical}}(1+z) = L_0 l[z] (1+z). \quad (4)$$

$$\sigma[z] = (1+z)^{2-d} l^{2-d}[z] \quad (5)$$

**Evolution in number density**

$$n[z] = n_0 (l[z](1+z))^{2-d} h^{-1}[z]. \quad (6)$$

**Evolution of mass  $m[z]$  and column density  $s[z]$**

$$m[z] \frac{dz}{h[z]} = s[z] (1+z)^{-2} n[z] dz. \quad (7)$$

$$m[z] = s[z] n[z] h[z] (1+z)^{-2}. \quad (8)$$

# QUASAR ABSORPTION FORESTS: PHENOMENOLOGY

## Evolution exponents

$$n[z] = (1+z)^\gamma, \quad l[z] = (1+z)^\varepsilon, \quad s[z] = (1+z)^\sigma, \quad (9)$$

$$m[z] = (1+z)^\mu, \quad h[z] = (1+z)^\nu. \quad (10)$$

$$(\varepsilon + 1) \cdot (2 - d) = \gamma + \nu \quad (11)$$

$$\mu = \sigma + \nu + \gamma - 2 \quad (12)$$

**Pressure-confined aggregates of fixed mass and temperature in an expanding hot gas environment**

Duncan,R.C., Vishniac,E.T., Ostriker,J.P. 1991

Miralda-Escudé,Jordi, Rees,Martin J. 1993 :

$$3\lambda - d(\lambda + 1) = \begin{pmatrix} -5 & \text{adiabatic} \\ -3 & \text{isothermal} \end{pmatrix}. \quad (13)$$

The catalogues give

$$\gamma = 0.25 \dots 5.7 \quad \text{mainly } 1.5 \dots 2$$

$$\sigma = 0.25 \dots 1.7 \quad \text{I believe } 1 \dots 1.5$$

## QUASAR ABSORPTION FORESTS: CONCLUSIONS

- Einstein-deSitter:  $\nu = 3/2$ ,

$$(\varepsilon + 1)(2 - d) = 1.75 \dots 7.2, \text{ resp. } 3 \dots 3.5 \quad (14)$$

$$\mu = 0 \dots 7.4, \text{ resp. } 2.5 \dots 3.5 \quad (15)$$

That contradicts any model for the absorbers.

- Approximately constant mass and absorbers not contracting yield

$$\nu < 0 \quad (16)$$

- sheet-like absorbers (bubble walls) yield in addition

$$\nu = -\gamma \quad (17)$$

$\nu < 0$  for some time works only in a Friedmann-Lemaître universe with positive cosmological constant and curvature.

## UNIVERSAL BUBBLE STRUCTURE

- CfA survey  
Geller,M.J., Huchra,J.P. 1991
- Pancake scenario
- Domain walls  
Nambu,Y., Ishihara,H., Gouda,N., Sugiyama,N. 1991
- No voids seen in the line density

**Conclusion:** The forest lines are the bubble walls itself

**Bubble wall counts of**

Liebscher,D.-E., Priester,W., Hoell,J. 1992

Liebscher,D.-E., Priester,W., Hoell,J. 1992

**yield**

$$\lambda_0 \approx 1.066, \kappa_0 \approx 0.08, \Omega_0 \approx 0.014 \quad (18)$$

$$z_{\min} \approx 3.5, h_{\min}^2 \approx 0.4 \quad (19)$$

## References

- [1] ARNOWITT,R., ET AL. (EDS.) (1990):  
*Strings '89*, World Scientific, Singapore.
- [2] ASHMAN,KEITH M. (1992): Dark matter in galaxies, *PAS Pacific* **104**, 1109-1138.
- [3] BAHCALL,NETA A., CEN,RENYUE (1992): Galaxy clusters and cold dark matter: a low-density unbiased universe? *Astrophys.J.Letters* **398**, L81-L84.
- [4] BENGSTON,INGEMAR, BOSTRÖM,OLAF (1992): Infinitely many cosmological constants, *Class.Quant.Grav.* **9**, L47-L51.
- [5] BEREZINSKY,V.S., GUREVICH,A.V., ZYBIN,K.P. (1992): Distribution of Dark Matter in the Galaxy and the Lower Limits for the Masses of Supersymmetric Particles, *Phys.Lett. B* **294**, 221-228.
- [6] BINNEY,JAMES (1992): Dark matter versus magnetism, *Nature* **360**, 624.
- [7] BRAINERD,T.G., VILLUMSEN,J.V. (1992): The Spatial Correlation Properties of Galaxy Halos in a Cold Dark Matter Universe, *Astrophys.J.* **400**, 398-409.
- [8] BRAINERD,T.G., VILLUMSEN,J.V. (1992): The Mass Function of Galaxy Halos in a Cold Dark Matter Universe, *Astrophys.J.* **394**, 409-421.
- [9] CALDWELL,D.O. (1992): Review of Dark Matter Experiments, *NP B Suppl.* **28A**, 273-279.
- [10] CARLBERG,R.G. (1991): A limit on the cosmological constant, *Astrophys.J.* **375**, 429-431.
- [11] CARROLL,S.M., PRESS,W.H., TURNER,E.L. (1992): The cosmological constant, *Astron.Nachr.* **30**, 499-542.
- [12] DAR,A. (1992): Tests of General Relativity and Newtonian Gravity at Large Distances and the Dark Matter Problem, *NP B Suppl.* **28A**, 321-326.
- [13] DAVIS,M., EFSTATHIOU,G., FRENK,C.S., WHITE,S.D.M. (1992): The end of cold dark matter? *Nature* **356**, 489-494.
- [14] DAVIS,M., SUMMERS,F.J., SCHLEGEL,D. (1992): Large-Scale Structure in a Universe with Mixed Hot and Cold Dark Matter, *Nature* **359**, 393-396.
- [15] DEKEL,A., SILK,J. (1986): The origin of dwarf galaxies, cold dark matter, and biased galaxy formation, *Astrophys.J.* **303**, 39-55.
- [16] DOMENECH,G., LEVINAS,M., UMEREZ,N. (1991): Classical supersymmetric matter and cosmology, *Gen.Rel.Grav.J.* **23**, 683-690.
- [17] DUNCAN,R.C., VISHNIAC,E.T., OSTRIKER,J.P. (1991): Expansion-cooled Lyman-alpha clouds, *Astrophys.J. L* **368**, L1-L6.
- [18] EFSTATHIOU,G., SUTHERLAND,W.J., MADDOX,S.J. (1990): The cosmological constant and cold dark matter, *Nature* **348**, 705-707.
- [19] EINASTO,JAAN, HAUD,URMAS, JOEVEER,MIHKEL, KAASIK,ANTS (1976): The Magellanic Stream and the mass of our Hypergalaxy, *Monthly Notices R.A.S.* **177**, 357-375.
- [20] ELLIS,J., LOPEZ,J.L., NANOPoulos,D.V. (1990):  
*Phys.Lett. B* **247**, 257.
- [21] FAHR,H.J. (1990): The Maxwellian alternative to the dark matter problem in galaxies, *Astron.Astroph.* **236**, 86-94.
- [22] FRIEMAN,J.A., GIUDICE,G.F. (1989): *Phys.Lett. B* **224**, 125.
- [23] FUKUGITA,M., FUTAMASE,T., KASAI,M. (1990): A possible test for the cosmological constant with gravitational lenses, *Monthly Notices R.A.S.* **246**, 24p-27p.
- [24] FUKUGITA,M., LAHAV,O. (1991): Ly $\alpha$  clouds at low redshift and the cosmological constant, *Monthly Notices R.A.S.* **253**, 17p-20p.

- [25] FUKUGITA,M., TAKAHARA,F., YAMASHITA,K., YOSHII,Y. (1990): Test for the cosmological constant with the number count of faint galaxies, *Astrophys.J.* **361**, L1-L4.
- [26] GELLER,M.J., HUCHRA,J.P. (1991): Mapping the universe, *ST* **82**, 134-139.
- [27] GELMINI,G.B. (1992): Dark Matter Particle Candidates, *NP B Suppl.* **28A**, 254-266.
- [28] GERHARD,O.E., SPERGEL,D.N. (1992): Dwarf Spheroidal Galaxies and Non-Newtonian Gravity, *Astrophys.J.* **397**, 38-43.
- [29] GESSNER,E. (1992): Cosmological Constant and the Flat Rotation Curves of Galaxies, *Astroph.Space Sci.* **194**, 197-205.
- [30] GRADWOHL,B.A., FRIEMAN,J.A. (1992): Dark Matter, Long-Range Forces, and Large-Scale Structure, *Astrophys.J.* **398**, 407-424.
- [31] GUTH,ALAN H. (1981): Inflationary universe: A possible solutionto the horizon and the flatness problems, *Phys.Rev. D* **23**, 347-356.
- [32] HAGELIN,J.S., PARKER,R.J.D. (1990): The effects of cold dark matter in standard big bangnucleosynthesis, *NP B* **329**, 464-492.
- [33] HODGES,H.M. (1993): Mirror Baryons as the Dark Matter, *Phys.Rev. D* **47**, 456-459.
- [34] HUT,P., REES,M.J. (1992): Constraints on Massive Black Holes as Dark Matter Candidates, *Monthly Notices R.A.S.* **259**, P27-P30.
- [35] KARDASHOV,N.S. (1990): Optimistic cosmological model, *Monthly Notices R.A.S.* **243**, 252-256.
- [36] KAUFFMANN,G., WHITE,S.D.M. (1992): The Observational Properties of an Omega = 0.2 Cold Dark Matter Universe, *Monthly Notices R.A.S.* **258**, 511-520.
- [37] KELLERMANN,K.I. (1993): The cosmological deceleration parameter estimated from the angular-size/redshift relation for compact radio sources, *Nature* **361**, 134-136.
- [38] KOCHANEK,C.S. (1992): Do the redshifts of gravitational lens galaxies rule out a large cosmological constant? *Astrophys.J.* **384**, 1-11.
- [39] KOLB,E.W., SECKEL,D., TURNER,M.S. (1985): The shadow world of superstring theories, *Nature* **314**, 415-419.
- [40] LAHAV,O., LILJE,P.B., PRIMACK,J.R., REES,M.J. (1991): Dynamical effects of the cosmological constant, *Monthly Notices R.A.S.* **251**, 128-136.
- [41] LIEBSCHER,D.-E., PRIESTER,W., HOELL,J. (1992): A new method to test the model of the universe, *Astron.Astroph.* **261**, 377-381.
- [42] LIEBSCHER,D.-E., PRIESTER,W., HOELL,J. (1992): Lyman alpha forests and the evolution of the universe, *Astron.Nachr.* **313**, 265-273.
- [43] MARKOV,M.A. (1993): The Problem of Dark Matter and Stable Elementary Black Holes (Maximons), *Phys.Lett. A* **172**, 331-332.
- [44] MATTEUCCI,F. (1992): The Influence of Dark Matter on the Chemical Evolution of Elliptical Galaxies, *Astrophys.J.* **397**, 32-37.
- [45] MIRALDA-ESCUDÉ,JORDI, REES,MARTIN J. (1993): Tests for the minihalo model of the Lyman alpha forest, *Monthly Notices R.A.S.* **260**, 617-624.
- [46] NAMBU,Y., ISHIHARA,H., GOUDA,N., SUGIYAMA,N. (1991): Anisotropies of the cosmic background raiation by domain wall networks, *Astrophys.J. L* **373**, L35-L37.
- [47] NINKOVICH,S., CHERNIN,A., SHAKENOV,M. (1990): Dark matter and dynamics of the local group, *Pisma Astron.Zh.* **16**, 1059-1065.
- [48] PEEBLES,P.J.E., SCHRAMM,D.N., TURNER,E.L., KRON,R.G. (1991): The case for the relativistic hot big bang cosmology, *Nature* **352**, 769-776.

- [49] PERSIC,MASSIMO, SALUCCI,PAOLO (1992): The baryon content of the universe, *Monthly Notices R.A.S.* **258**, 14p-18p.
- [50] SACKETT,P.D., SPARKE,L.S. (1990): The dark halo of the polar-ring galaxy NGC 4650A, *Astrophys.J.* **361**, 408-418.
- [51] SCHRAMM,D. (1991): Late-time cosmological phase transition, *=SAJ91* , 225-242.
- [52] SCHRAMM,D.N. (1992): Dark Matter and Cosmology, *NP B Suppl.* **28A**, 243-253.
- [53] SCIAMA,D.W. (1990):  
*Comm.Astrophys.* **15**, 71.
- [54] SILK,J., JUSZKIEWICZ,R. (1991): Cosmology: Texture and cosmic structure, *Nature* **353**, 386-388.
- [55] STUBBS,C.W. (1993): Experimental Limits on Any Long Range Nongravitational Interaction Between Dark Matter and Ordinary Matter, *Phys.Rev.Lett.* **70**, 119-122.
- [56] TAYLOR,A.N., ROWAN-ROBINSON,M. (1992): The Spectrum of Cosmological Density Fluctuations and Nature of Dark Matter, *Nature* **359**, 396-399.
- [57] TURNER,EDWIN L., IKEUCHI,SATORU (1992): Quasar absorption lines with a non-zero cosmological constant, *Astrophys.J.* **389**, 478-490.
- [58] TURNER,M.S. (1990): *Phys.Rep.* **197**, 67.
- [59] VANDALEN,A., SCHAEFER,R.K. (1992): Structure Formation in a Universe with Cold Plus Hot Dark Matter, *Astrophys.J.* **398**, 33-42.